

Interactive Tutorial System for Linear Circuit Analysis: Impact on Learning and Novel Tutorials

Introduction

• Linear circuit analysis is a foundational topic for electrical engineering students and frequently comprises the exposure to electrical topics for non-electrical engineers. Increasing success in this course is therefore important to improving graduation and retention rates

• This approach involves random problem generation using special algorithms (varying the structure of the circuit, not just element values), and automatic generation of fully worked and explained solutions using normal textbook methods (rather than numerical approaches as in PSPICE, etc.)

This system provides step-based tutoring, where every phase of a student's work is immediately checked for accuracy using special interfaces to accept re-drawn or edited circuit diagrams, equations (using special template-based interfaces), interactively sketched waveforms as a function of time, simplified equation and matrix entry forms, etc.

• The well known advantages of studying worked examples in the early stages of learning^{1,2} are exploited in this system, where the examples are designed to be isomorphic to the problems

• Typical misconceptions and qualitative skills are targeted, such as identification of elements in series and parallel

The software is adaptive to the needs of individual students, providing more or less practice and explanation in each case as needed by individual students



Comparison with Publisher-Based Homework System (Fall 2015)

• Prior trials of this system showed a large, statistically significant advantage over paper homework (e.g., Cohen *d*-value, based on difference of post-test scores of 1.21 σ in a laboratory-based trial in Fall 2013 with p < 0.05) and higher assignment scores and student preferences over a publisher-based system in Fall 2014 (p < 0.008 with an effect size of $d = 0.41 \sigma$) • A second randomized, controlled classroom-based evaluation was conducted in Fall 2015 (similar to the one in Fall 2014), where students were randomly assigned to either A) use Circuit Tutor for nodal analysis, and the publisher system (denoted "System X") for mesh analysis; or B) the opposite. On the assignment due date, a post-test (quiz) was given in class on both topics to the total of ~70 students (not performed in Fall 2014). An anonymous survey was also administered asking them to compare Circuit Tutor to System X.

• Students using Circuit Tutor had a statistically significant higher post-test score than those using System X on node analysis (Table I), with [t(64) = 3.09, p < 0.05] with an effect size (Cohen *d*-value) of 0.72σ . For mesh analysis, the difference was not statistically significant [t(64) = 0.88, p = 0.38], which may reflect the fundamentally easier nature of that topic (both groups had relatively high averages).

• Large majorities also preferred Circuit Tutor over System X and felt that it taught them more effectively (Table I). • A typical student comment was "I liked Circuit Tutor more because I could do a ton of problems. I liked that even if I couldn't figure it out, I could 'give up'; and it would thoroughly explain how to do everything so I could understand what I did wrong and then do a new problem and try to get that right. I seem to retain more of the content when I am doing this one. I have trouble with [System X] because, if I have trouble with a problem, the hints do not explain what I am doing wrong. It's really frustrating because I could be 2 or 3 wrong attempts in and I do not know what I'm doing wrong."

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		Por	tions of a
Problem			
Draw a Bode magn	itude plot for the transfer functio	n	
	$\mathbf{H}(j\omega)$	$0 = \frac{4000 (j\omega + 2)}{j\omega \left[(j\omega)^2 + 8j\omega + 400 \right]}.$	
Solution:			
Step 1: Rewrite the Note: In standard fo	transfer function in standard rm, the constant of each term is	form. unity.	
	$\mathbf{H}(j\omega) =$	$\frac{4000 (j\omega + 2)}{j\omega \left[(j\omega)^2 + 8j\omega + 400 \right]}$	
	=	$\frac{4000 \cdot 2 \cdot \left(\frac{j\omega}{2} + 1\right)}{400 \cdot j\omega \left[\frac{(j\omega)^2}{400} + \frac{8}{400}j\omega + 1\right]}$	
	=	$\frac{20\left(1+\frac{j\omega}{2}\right)}{j\omega\left[1+0.02j\omega+\left(\frac{j\omega}{2\pi}\right)^2\right]}.$	
Step 2: Identify the This transfer function • A constant coe • A pole at the o • A simple zero • A pair of comp	terms making up the transfer n has the following terms: efficient with an value of 20 = 20 rigin at a break frequency of ω = 2 ra lex conjugate poles at a break fr	function. log(20) dB = 26 dB d/s requency of ω = 20 rad/s	
Hint: Poles are term	s in the denominator involving <i>ja</i>	 and zeros are terms in the num 	erator involving <i>jω</i> .
Step 3: Find the co	mplex magnitude of the trans	fer function.	Rules for
✓ Details of Finding	ng H(jω)]		
The magnitude of a origin). Thus, $ \mathbf{z} ^2$ = negative! Further, multiplication of co the magnitude of e following terms we sum of all terms the	a complex number $\mathbf{z} = x + jy$ is $ \mathbf{z} = x^2 + y^2$. As <i>x</i> and <i>y</i> are real num $ \mathbf{z}_1/\mathbf{z}_2 = \mathbf{z}_1 / \mathbf{z}_2 $ and $ \mathbf{z}_1\mathbf{z}_2 = \mathbf{z}_1 $ mplex numbers in polar form. The each term and then multiply or dimension first evaluate $j^2 = -1$. Then we at multiplying <i>j</i> as the imaginary	$ \mathbf{z} = \sqrt{x^2 + y^2}$ (the distance of the purpose of the parameters, the definition implies that a $ \mathbf{z}_2 $, which are easily seen from the therefore, finding the magnitude of vide the magnitudes of those term identify the sum of all numbers not part, by definition.	point z in the complete complex magnitude he procedures for d $\mathbf{H}(j\omega)$ requires that as as appropriate. For bot multiplying <i>j</i> as th
Term	Real Part	Imaginary Part	Magnitude
jω	0	ω	ω
		(1)	

Term	Real Part	Imaginary Part	Magnitude
jω	0	ω	ω
$1 + \frac{j\omega}{2}$	1	$\frac{\omega}{2}$	$\sqrt{1+\left(\frac{\omega}{2}\right)}$
$1 + 0.02j\omega + \frac{(j\omega)^2}{400}$	$1 - \frac{\omega^2}{400}$	0.02 <i>w</i>	$\sqrt{\left(1-\frac{\omega^2}{400}\right)}$

Usage Data and Survey Results

• A total of 18 different tutorials are now available, covering identification of series & parallel circuit elements (including the case when terminals are present); simplification of resistors, inductors, capacitors, and general impedances in series & parallel, including complicated, multi-step sequences; both DC and AC steady-state node and mesh analysis, including full solutions of those problems; the mathematics of direct and inverse Laplace transforms; construction of Bode plots from transfer functions; and interactive sketching of waveforms such as current, voltage, power, and energy as a function of time for general electrical properties and for inductors and capacitors • A total of over 2860 students in 71 class sections at 10 different colleges and universities of widely varying types have used the system to date, usually as required homework. Institutions have included Arizona State University, University of Notre Dame, University of the Pacific, Morgan State University, Auburn University, Messiah College, North Carolina A&T State University, University of Virginia, South Mountain Community College, Chandler-Gilbert Community College, and Glendale Community College

• In surveys at time of module completion, students were asked to rate the tutorial as "very useful," somewhat useful," "not very useful," or "a waste of time." For the most recent year Spring 2015-Fall 2015, the responses in each category (combining all tutorials) were 65%, 26%, 4%, and 5%, respectively, for a total of 91% favorable (very or somewhat useful).

• Ratings from a more detailed, anonymous survey administered at the end of each semester were also generally favorable as shown in Table II

Effects on Student Learning and Preferences							
able I. Results of Classroom-Based Experiment in Fall 2015.							
System used	Circuit Tutor	System X					
Mean post-test score-node analysis (std. dev.)	72%(24%)	49%(33%)					
Mean post-test score-mesh analysis (std. dev.)	71%(25%)	65%(31%)					
Mean node/mesh HW score	79%	69%					
Preferred system in question	86%	9%*					
Felt system in question taught more effectively	94%	3%*					
Remaining students rated both systems equal							

Table II. Percentag

Institution Arizona State U Morgan State U Univ. of the Pac Messiah College Univ. of Notre I All (combined)

References

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Software Survey Results (End of Semester)

ge of Favorable Scores on End-of-Semester Survey by Institution							
		Appropriate.	Prefer to				
	Useful & well	difficulty &	conventional				
1	designed	coverage	homework	Overall	N		
niv.	80.0%	78.6%	78.5%	79.0%	841		
niv.	78.1%	70.1%	79.5%	75.9%	56		
ific	69.4%	71.1%	53.3%	64.6%	45		
e	87.1%	91.4%	82.8%	87.1%	58		
Dame	91.8%	91.9%	87.9%	90.5%	31		
	80.1%	78.7%	77.8%	78.9%	1031		

For Further Information or to Use this Software in Your Classes

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Inverse Laplace Transform (Computer-Generated)

 $(s + 10)(s^2 + 10s + 29)$ The first step is to factor the quadratic terms in **F**(s). For the general quadratic equation $as^2 + bs + c = 0$, the roots are given by $\mathbf{s}_{1,2} = \frac{-b}{2a} \pm \sqrt{\left(\frac{b}{2a}\right)^2 - \frac{c}{a}},$

 $(s - s_1)(s - s_2) = 0.$

 $\mathbf{s}_{1,2} = \frac{-(10)}{2} \pm \sqrt{\left(\frac{10}{2}\right)^2 - 29}$

 $s^{2} + 10s + 29 = (s + 5 - j2)(s + 5 + j2).$

5(s + 40) $\mathbf{F}(\mathbf{s}) = \frac{1}{(\mathbf{s}+10)(\mathbf{s}+5-j2)(\mathbf{s}+5+j2)}$

 $\mathbf{F}(\mathbf{s}) = \frac{k_0}{\mathbf{s} + p_0} + \frac{\mathbf{k}_1}{\mathbf{s} + \mathbf{p}_1} + \frac{\mathbf{k}_1^*}{\mathbf{s} + \mathbf{p}_1^*},$

 $\mathbf{k}_i = (\mathbf{s} + p_i)\mathbf{F}(\mathbf{s})\Big|_{\mathbf{s} = -p_i}.$

5(s + 40) $(s+10)(s+5-j2)(s+5+j2)|_{s=-10}$



Web-Based Waveform Sketching Tool Section 2 of 3



Add segment:





Vertical Axis Settings Check Graph

Equation



Conclusions

• Recently added features include automatic generation of voltage and current division equations; new tutorials featuring interactive waveform sketching of electrical quantities; Laplace and inverse Laplace transform tutorials where students interactively complete exercises using a template-based system; and problem and solution generation involving superposition and switches for transient circuits

• Over 2860 students have used the software to date in 71 class sections at ten different colleges and universities of various types

• Student satisfaction has been high at various institutions and students strongly prefer the system to a commercial, publisher-based system

• A new controlled, randomized classroom-based trial in Fall 2015 showed a statistically significant advantage of 0.72σ for nodal analysis taught by Circuit Tutor as compared to a commercial, publisher-based system; results for mesh analysis were not significantly different

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